

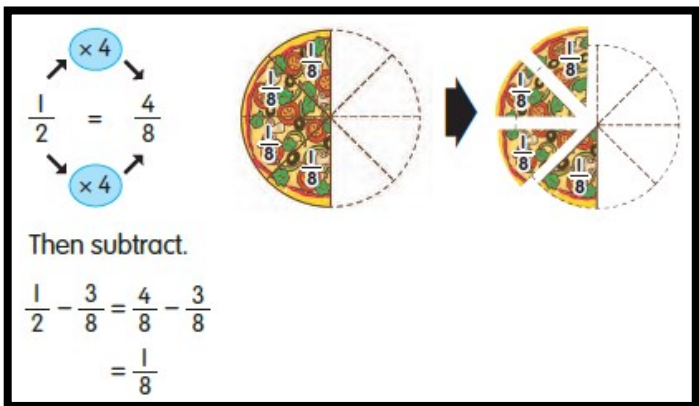
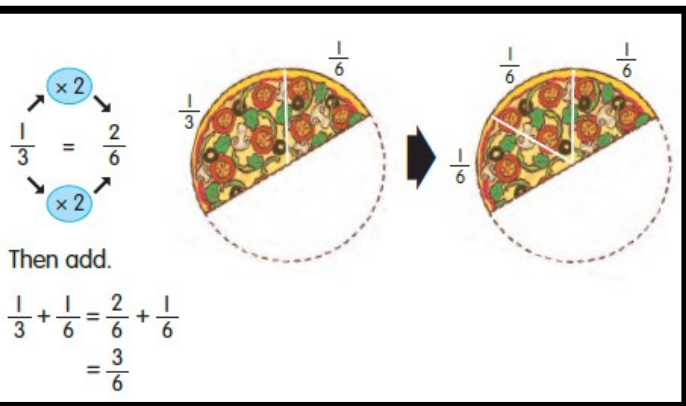
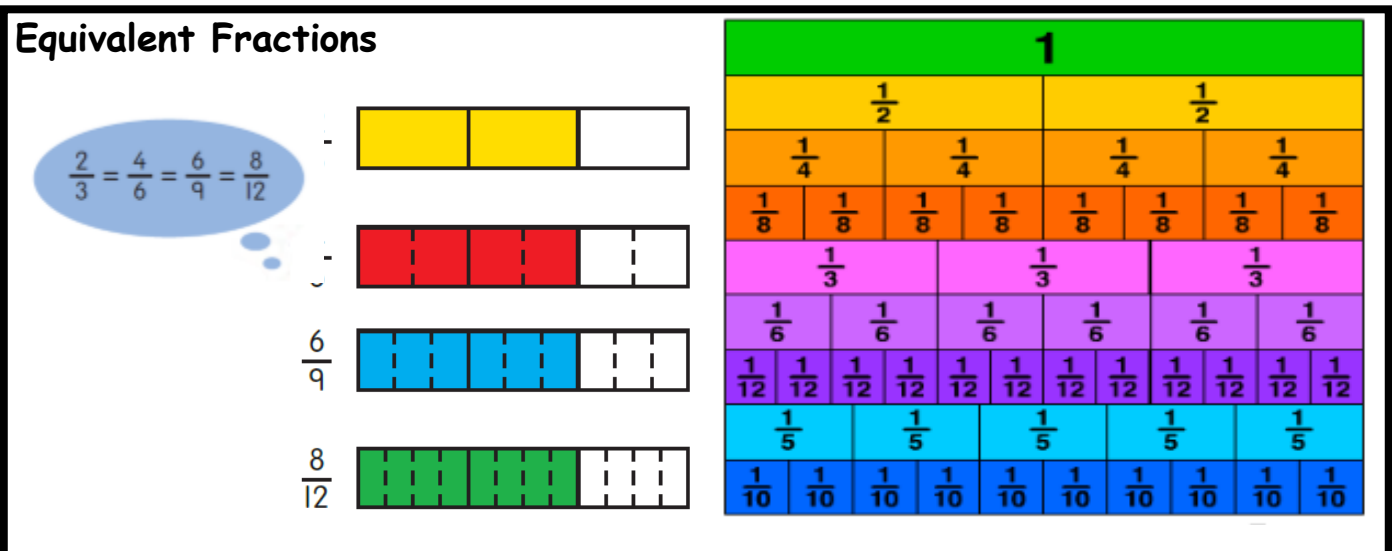
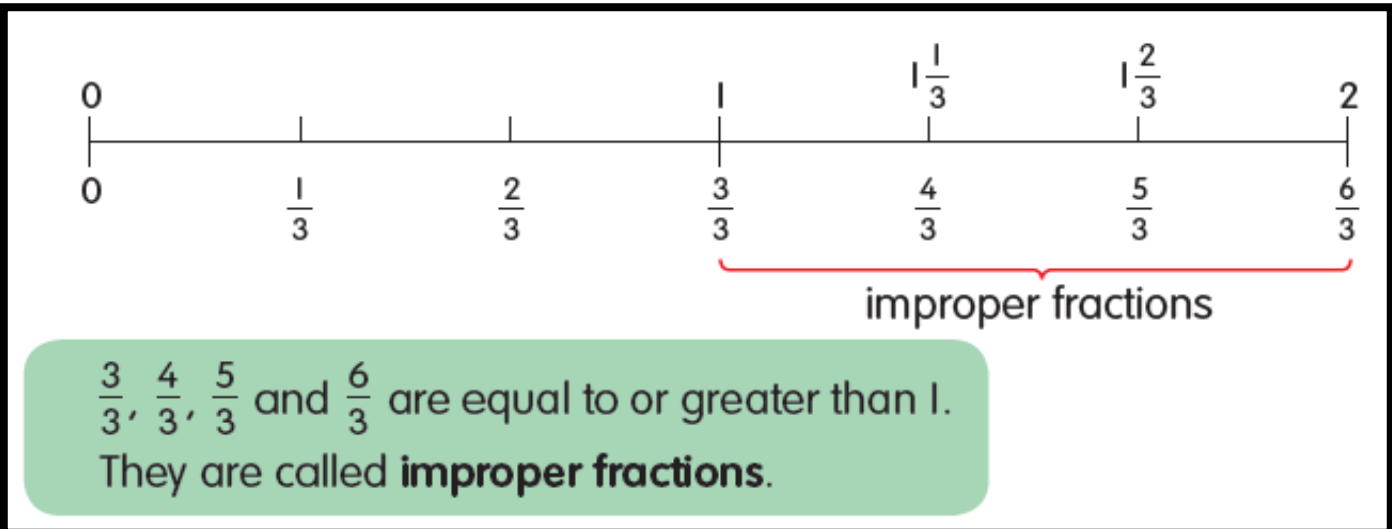
# **MATHS SPRING 2 KNOWLEDGE ORGANISERS**



# Year 5 Unit 4—Fractions



<p><b>Equivalence</b></p> <p>Having the same value</p> $\frac{1}{2} = \frac{2}{4} = \frac{8}{16}$ $1 \div 2 = 0.5 \quad 2 \div 4 = 0.5 \quad 8 \div 16 = 0.5$	<p><b>Improper Fraction</b></p> <p>A fraction greater than one whole</p> $\frac{8}{5}$
<p><b>Proper Fraction</b></p> <p>A fraction smaller than one whole</p> $\frac{2}{3}$ $\frac{3}{10}$	<p><b>Mixed Number</b></p> <p>Written as a whole number and a proper fraction</p> $1\frac{3}{4} \frac{1}{4}$





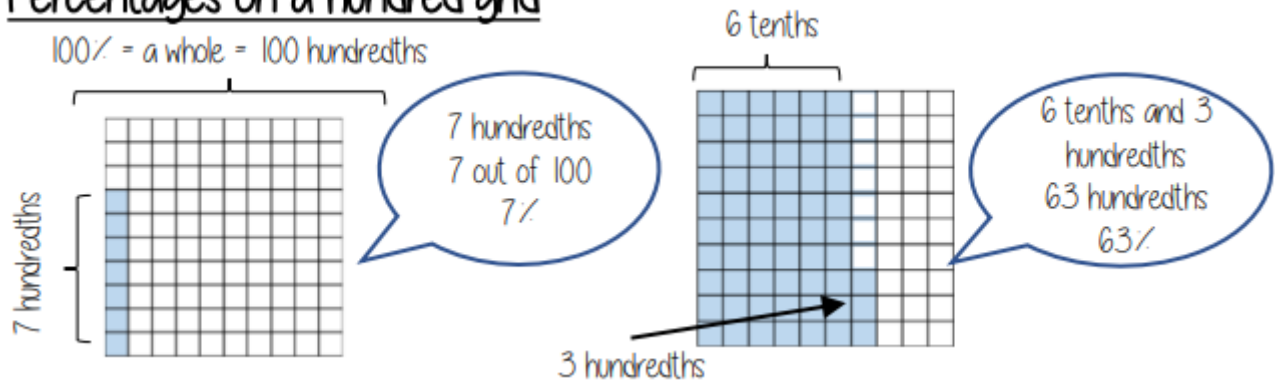
# Year 6 Unit 7

## Percentages

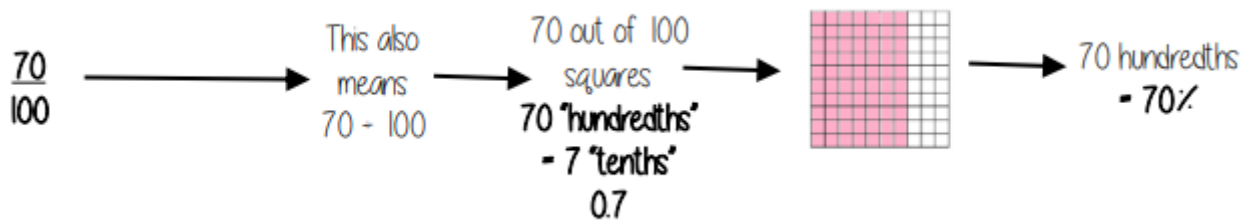


Percentage means out of 100

### Percentages on a hundred grid

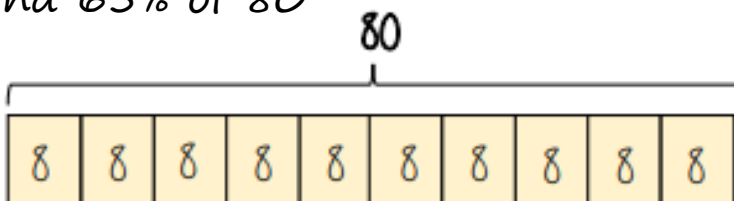


### Equivalence



Find the percentage of an amount using mental methods.

Find 65% of 80



For bigger percentages it is sometimes easier to take away from 100%

#### Method 1

$$\begin{aligned} 65\% &= (10\% \times 6) + 5\% \\ &= (8 \times 6) + 4 \\ &= 54 \end{aligned}$$

#### Method 2

$$\begin{aligned} 65\% &= 50\% + 10\% + 5\% \\ &= 40 + 10 + 4 \\ &= 54 \end{aligned}$$

# Year 6 Unit 8

## Metric Conversions

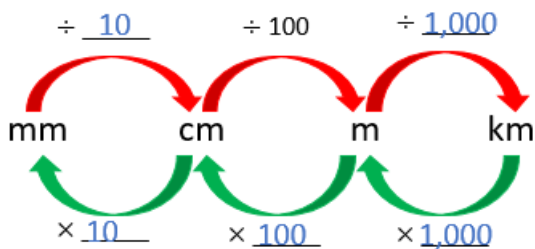


### Metric Units

Length	The measurement of something from end to end
Capacity	The maximum amount that something can contain
Mass	The amount of matter that makes up an object or substance

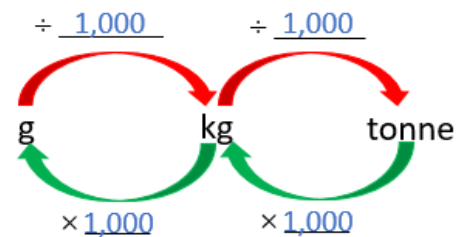
Length		Capacity	Mass
cm	km	ml	g    tonne
mm	m	l	kg

### Length



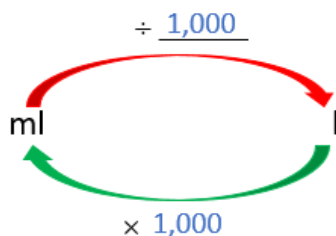
There are 10 millimetres in 1 centimetre.  
 There are 100 centimetres in 1 metre.  
 There are 1,000 metres in 1 kilometre.

### Mass



There are 1,000 grams in 1 kilogram.  
 There are 1,000 kilograms in 1 tonne.

### Capacity

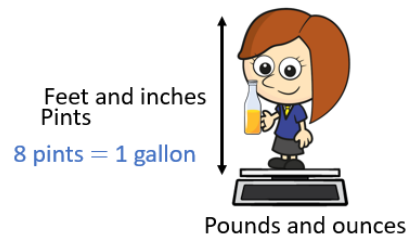


There are 1,000 millilitres in 1 litre.

*One thousandth*  
 One thousandth of a litre

### Imperial Measures

16 ounces = 1 pound  
 14 pounds = 1 stone



12 inches = 1 foot  
 1 inch  $\approx$  2.5 cm

5 miles  $\approx$  8 km  
 $\times 8$                        $\times 8$   
 40 miles  $\approx$  64 km

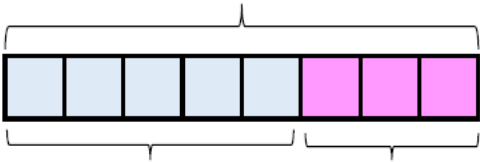


# Year 6 Unit 9—Ratio



**What is a ratio?** For every 5 Blues there are 3 pinks

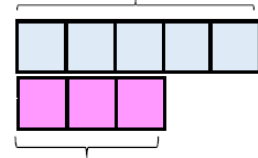
This is the 'whole' - blues and pinks together



This represents the 5 blues    This represents the 3 pinks

5:3

This represents the 5 blues



This is the 'whole' - blues and pinks together

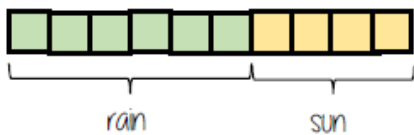
This represents the 3 pinks

**Simplifying a ratio**

Cancel down the ratio to its lowest form

"For every 6 days of rain there are 4 days of sun"

6:4



+ by 2 ↓

3:2



Find the biggest common factor that goes into all parts of the ratio

For 6 and 4 the biggest factor (number that multiplies into them is 2)

"For every 3 days of rain there are 2 days of sun" - when this happens twice the ratio becomes 6:4.

**Order is important**

"For every dog there are 2 cats"



1:2

The ratio has to be written in the same order as the information is given

@whisto\_maths

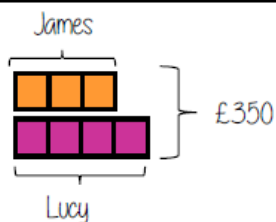
**Dividing into a given ratio**

James and Lucy share £350 in the ratio 3:4.  
Work out how much each person earns

Model the Question

James: Lucy

3 : 4



Find the value of one part

$$£350 \div 7 = £50$$

Whole: £350

7 parts to share between  
(3 James, 4 Lucy)

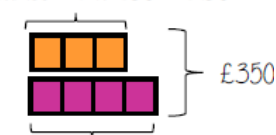
□ = one part  
= £50

Put back into the question

James: Lucy

(x 50) 3 : 4 (x 50)  
↳ £150 : £200

$$\text{James} = 3 \times £50 = £150$$

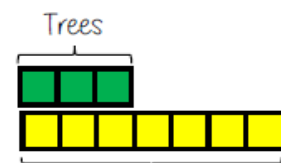


$$\text{Lucy} = 4 \times £50 = £200$$

**Ratio and fractions**

Trees: Flowers

3 : 7



Ratio

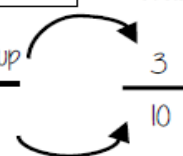
There are 3 parts for trees

Flowers

Fraction of trees

Number of parts of in group

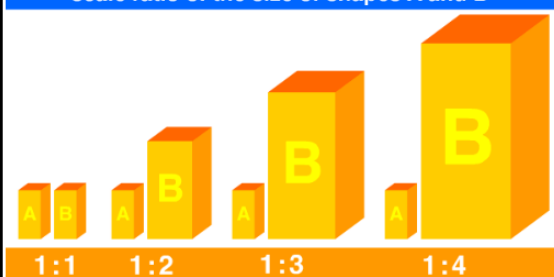
Total number of parts



Fraction

Tree parts 3 + Flower parts 7 = 10

scale ratio of the size of shapes A and B



# Year 7 Unit 6

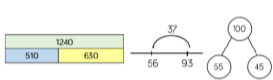
## Applying Addition and Subtraction



Addition	The joining of two or more numbers or quantities.	In <b>addition</b> two or more numbers are joined to get one number which is the <b>sum</b> or the <b>total</b> .
Sum Total	The result of adding; the whole amount	
Subtraction	When one quantity is taken away from another	80 <b>subtract</b> 30 is 50. The <b>difference</b> between 80 and 30 is 50
Difference	The result of subtracting one number from another	
Commutative	Numbers can be added in any order, but in subtraction the order is important.	$a + b = b + a$ $6 + 2 = 8$ or $2 + 6 = 8$
Associative	In addition, no matter how numbers are grouped, the answers will be same.	 $(6 + 3) + 4 = 6 + (3 + 4)$
Inverse	The reverse or opposite of an operation.	 $4 + 2 = 6$ $2 + 4 = 6$ $6 - 4 = 2$ $6 - 2 = 4$
Perimeter	The distance around a polygon.	 Perimeter = $2L + 2W$ Same as: $L + L + W + W$
Profit	Profit occurs when an item is sold for more than it cost to purchase.	
Loss	Loss occurs when an item is sold for less than it cost to purchase.	

### Addition and Subtraction

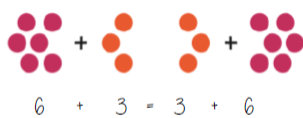
@whisto\_maths



Modelling methods for addition/ subtraction

- Bar models
- Number lines
- Part/ Whole diagrams

Addition is commutative



The order of addition does not change the result

Subtraction the order has to stay the same

$$360 - 147 = 360 - 100 - 40 - 7$$

- Number lines help for addition and subtraction
- Working in 10's first aids mental addition/ subtraction
- Show your relationships by writing fact families

Formal written methods

	H	T	O
+	1	8	7
+	5	4	2

	H	T	O
		4	2
-		2	4
			9

Remember the place value of each column. You may need to move 10 ones to the ones column to be able to subtract

### Addition and Subtraction of decimals

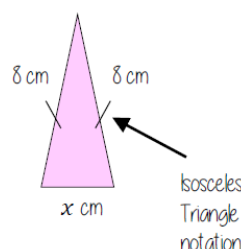
4	.	3	8
7	.	9	0
			+

0 can be used to fill empty places with value

The decimal place acts as the placeholder and aligns the other values

### Perimeter problems

Perimeter is the length around the outside of a polygon



The triangle has a perimeter of 25cm. Find the length of  $x$

$$8\text{cm} + 8\text{cm} + x\text{cm} = 25\text{cm}$$

$$16\text{cm} + x\text{cm} = 25\text{cm}$$

$$x\text{cm} = 9\text{cm}$$

# Year 7 Unit 7

## Applying Multiplication and Division



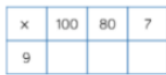
Product	The result when two numbers are multiplied.	$6 \times 3 = 18$ Factor      Factor      Product
Factor	Numbers we can multiply together to get another number.	
Multiple	The result of multiplying a number by a positive whole number	6, 12, 18, 20, 24 ..... are all multiples of 6
Commutative	Numbers can be multiplied in any order, but in division the order is important.	$2 \times 4 = 8$ $4 \times 2 = 8$
Inverse	The reverse or opposite of an operation.	

### Multiplication methods

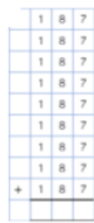
@whisto\_maths



Long multiplication (column)



Grid method



Repeated addition

Less effective method especially for bigger multiplication

#### Multiplication with decimals

Perform multiplications as integers  
 eg  $0.2 \times 0.3 \longrightarrow 2 \times 3$

Make adjustments to your answer to match the question:  
 $0.2 \times 10 = 2$   
 $0.3 \times 10 = 3$

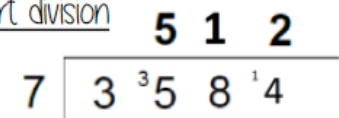
Therefore  $6 \div 100 = 0.06$

Estimations: Using estimations allows a 'check' if your answer is reasonable

### Division methods

$$3584 \div 7 = 512$$

Short division

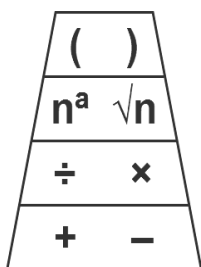


Complex division

$$\div 24 = \div 6 \div 4$$

Break up the divisor using factors

### Order of Operations



Brackets

Powers /Indices

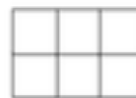
Multiplication or Division

Addition or Subtraction

### Area

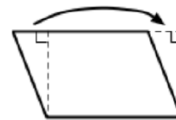
Rectangle

Base x Perpendicular height



Parallelogram/ Rhombus

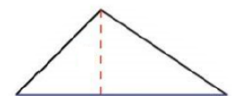
Base x Perpendicular height



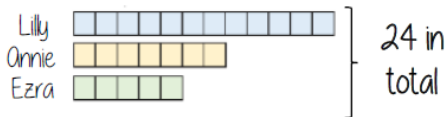
Triangle

$\frac{1}{2} \times \text{Base} \times \text{Perpendicular height}$

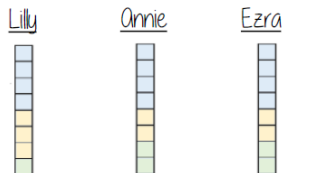
A triangle is half the size of the rectangle it would fit in



### Mean problems



Finding the mean amount is the average amount each person would have if shared out equally



The mean number of blocks would be 8 each

### Multiply by powers of 10



$$3 \times 100 = 300$$





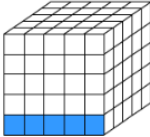
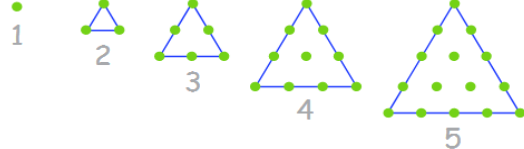
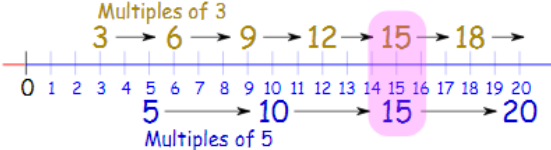
$$0.03 \times 100 = 3$$



# Year 8 Unit 6

## Prime Numbers and Proof



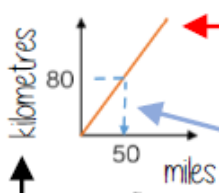
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Factor	Numbers we can multiply together to get another number.																																																																																																					
Multiple	The result of multiplying a number by a positive whole number	6, 12, 18, 20, 24 ..... are all multiples of 6																																																																																																				
Square Number	To square a number: just multiply it by itself. 4 squared is $4 \times 4 = 16$ . Often shown with a little 2 in the corner like this: $4^2 = 16$ that is said "4 squared equals 16"	$4$  $2^2$ or $2 \times 2 = 4$ $9$  $3^2$ or $3 \times 3 = 9$																																																																																																				
Cube Number	The result of using a whole number in a multiplication three times.	 $5 \times 5 \times 5 = 125$ so $5^3 = 125$																																																																																																				
Triangular Number	A number that can make a triangular dot pattern. 1, 3, 6, 10, 15	1 dot    3 dots    6 dots    10 dots    15 dots 																																																																																																				
Lowest Common Multiple	The smallest number that is the multiple of two or more other numbers.	 15 is the lowest common multiple (LCM) of 3 and 5																																																																																																				
Highest Common Factor	The highest number that is a factor of two or more numbers.	Factors of 12: 1, 2, 3, 4, 6, 12 Factors of 16: 1, 2, 4, 8, 16 Common Factors 4 is the highest common factor (HCF) of 12 and 16																																																																																																				
Prime Numbers	A whole number <b>greater than 1</b> that can not be made by multiplying other whole numbers. They only have 2 factors; one and themselves	<p style="text-align: center; background-color: #0056b3; color: white; padding: 2px;">prime numbers to 100</p> <table border="1" style="width: 100%; text-align: center; border-collapse: collapse;"> <tr><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td><td>6</td><td>7</td><td>8</td><td>9</td><td>10</td></tr> <tr><td>11</td><td>12</td><td>13</td><td>14</td><td>15</td><td>16</td><td>17</td><td>18</td><td>19</td><td>20</td></tr> <tr><td>21</td><td>22</td><td>23</td><td>24</td><td>25</td><td>26</td><td>27</td><td>28</td><td>29</td><td>30</td></tr> <tr><td>31</td><td>32</td><td>33</td><td>34</td><td>35</td><td>36</td><td>37</td><td>38</td><td>39</td><td>40</td></tr> <tr><td>41</td><td>42</td><td>43</td><td>44</td><td>45</td><td>46</td><td>47</td><td>48</td><td>49</td><td>50</td></tr> <tr><td>51</td><td>52</td><td>53</td><td>54</td><td>55</td><td>56</td><td>57</td><td>58</td><td>59</td><td>60</td></tr> <tr><td>61</td><td>62</td><td>63</td><td>64</td><td>65</td><td>66</td><td>67</td><td>68</td><td>69</td><td>70</td></tr> <tr><td>71</td><td>72</td><td>73</td><td>74</td><td>75</td><td>76</td><td>77</td><td>78</td><td>79</td><td>80</td></tr> <tr><td>81</td><td>82</td><td>83</td><td>84</td><td>85</td><td>86</td><td>87</td><td>88</td><td>89</td><td>90</td></tr> <tr><td>91</td><td>92</td><td>93</td><td>94</td><td>95</td><td>96</td><td>97</td><td>98</td><td>99</td><td>100</td></tr> </table>	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40	41	42	43	44	45	46	47	48	49	50	51	52	53	54	55	56	57	58	59	60	61	62	63	64	65	66	67	68	69	70	71	72	73	74	75	76	77	78	79	80	81	82	83	84	85	86	87	88	89	90	91	92	93	94	95	96	97	98	99	100
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# Year 8 Unit 8 Multiplicative Change



Proportion	A statement that links two ratios
Variable	A part where the value can be changed
Scale Factor	The multiple that increases or decreases a shape in size
Conversion	The process of changing one variable to another

## Conversion Graphs



This is always a straight line because as one variable increases so does the other at the same rate

To make conversions between units you need to find the point to compare – then find the associated point by using your graph  
Using a ruler helps for accuracy  
Showing your conversion lines help as a "check" for solutions

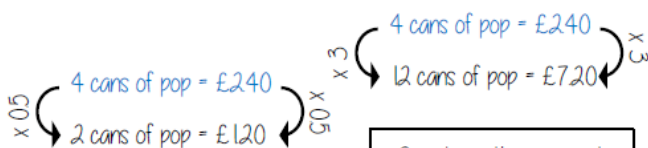
Labelling of both axes is vital

## Direct Proportion

As one variable changes the other changes at the same rate



4 cans of pop = £2.40



This multiplier is the same in the same way that this would be for ratio

Sometimes this is easiest if you work out how much one unit is worth first  
e.g. 1 can of pop = £0.60

## Ratio in similar shapes

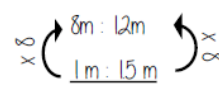
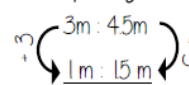


Angles in similar shapes do not change.  
e.g. if a triangle gets bigger the angles can not go above  $180^\circ$

The two rectangles are similar.



Corresponding sides



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## Interpreting Scale Drawings

A picture of a car is drawn with a scale of 1:30

For every 1cm on my image is 30cm in real life

The car image is 10cm



The car in real life is 210cm



# Year 8 Unit 9

## Multiplying and Dividing Fractions



Unit Fractions	Fractions with a numerator of one,	$\frac{1}{2}$ $\frac{1}{4}$
Reciprocal	A pair of numbers that multiply together to give 1	<div style="display: flex; justify-content: space-around;"> <div style="text-align: center;"> <p>Fraction</p> <math>\frac{2}{3}</math> </div> <div style="text-align: center;"> <p>Reciprocal</p> <math>\frac{3}{2}</math> </div> </div> <p style="text-align: center;">→</p>

### Multiplying Unit Fractions

$$\frac{1}{4} \times \frac{1}{3} = \frac{1}{12}$$

Parts shaded

Modelled:

Total number of parts in the diagram

### Multiplying by an integer = repeated addition

$$4 \times \frac{2}{5} \rightarrow \frac{2}{5} + \frac{2}{5} + \frac{2}{5} + \frac{2}{5}$$

Integer (Whole number)

Each part represents  $\frac{1}{5}$

How many parts are shaded?  
What each part represents

$$= \frac{8}{5}$$

$$= 1 \frac{3}{5}$$

### Multiplying non-unit fractions

$$\frac{3}{4} \times \frac{2}{3} = \frac{6}{12}$$

Shade in 3 parts

Repeat it on this many rows

This many columns

This many rows

Modelled:

Total number of parts in the diagram

### Dividing by any fraction

$$\frac{2}{5} \div \frac{3}{4}$$

Multiplying by a reciprocal gives the same outcome

$$\frac{2}{5} \times \frac{4}{3}$$

Represented

$$= \frac{8}{5}$$

### Dividing an integer by a unit fraction

$$1 \div \frac{1}{4} = 4$$

How many quarters are in 1?

"There are 4 quarters in 1 whole. Therefore, there are 20 quarters in 5 wholes"

$$5 \div \frac{1}{4} = 20$$